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**MARTIN MARIETTA**  
**FLUID VISCOUS DAMPER STUDY**  
**OAK RIDGE PLANT**  
**BUILDING X-330**

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by

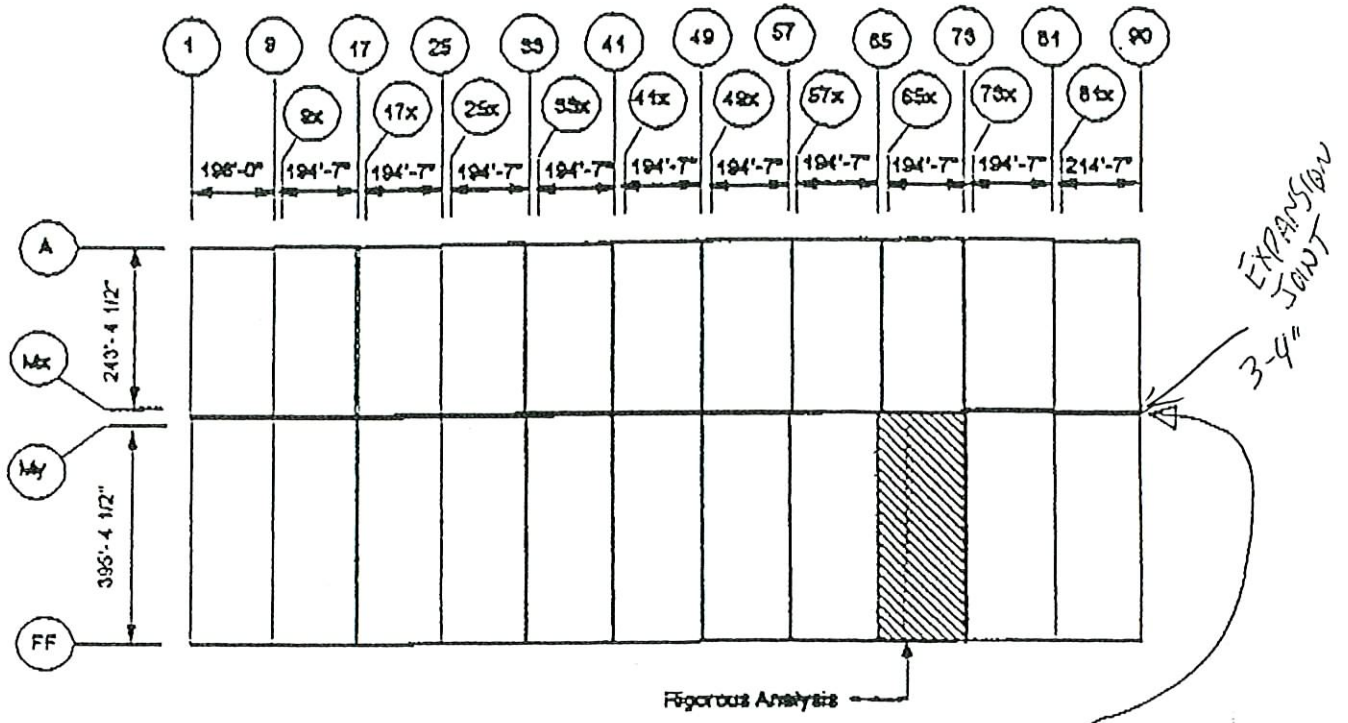
**Craig Winters**

**Taylor Devices, Inc.**  
90 Taylor Drive  
P.O. Box 748  
N. Tonawanda, NY 14120-0748

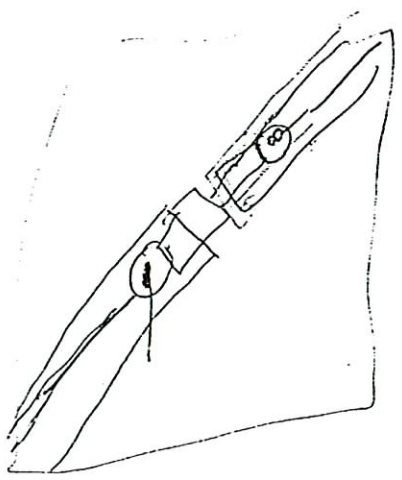
**January 16, 1995**

# **BUILDING INFORMATION**

**MARTIN MARIETTA  
OAK RIDGE PLANT  
BUILDING X-330**



Rocker Support  
between  
units along  
My line.



Plan View of Building X-330  
Figure 1.2.2-1

Description	Approx. Elevation	Weight (kips)	% of Total
Cell Floor	694'-0"	14883	81.54
1st Mezzanine	708'-0"	1673	9.17
Roof	737'-3"	1697	9.30

Total Weight of Building = 18253 kips

Grade Elevation is at 671'-0"

Building X-330 Mass Distribution

Table 3.1.3-3



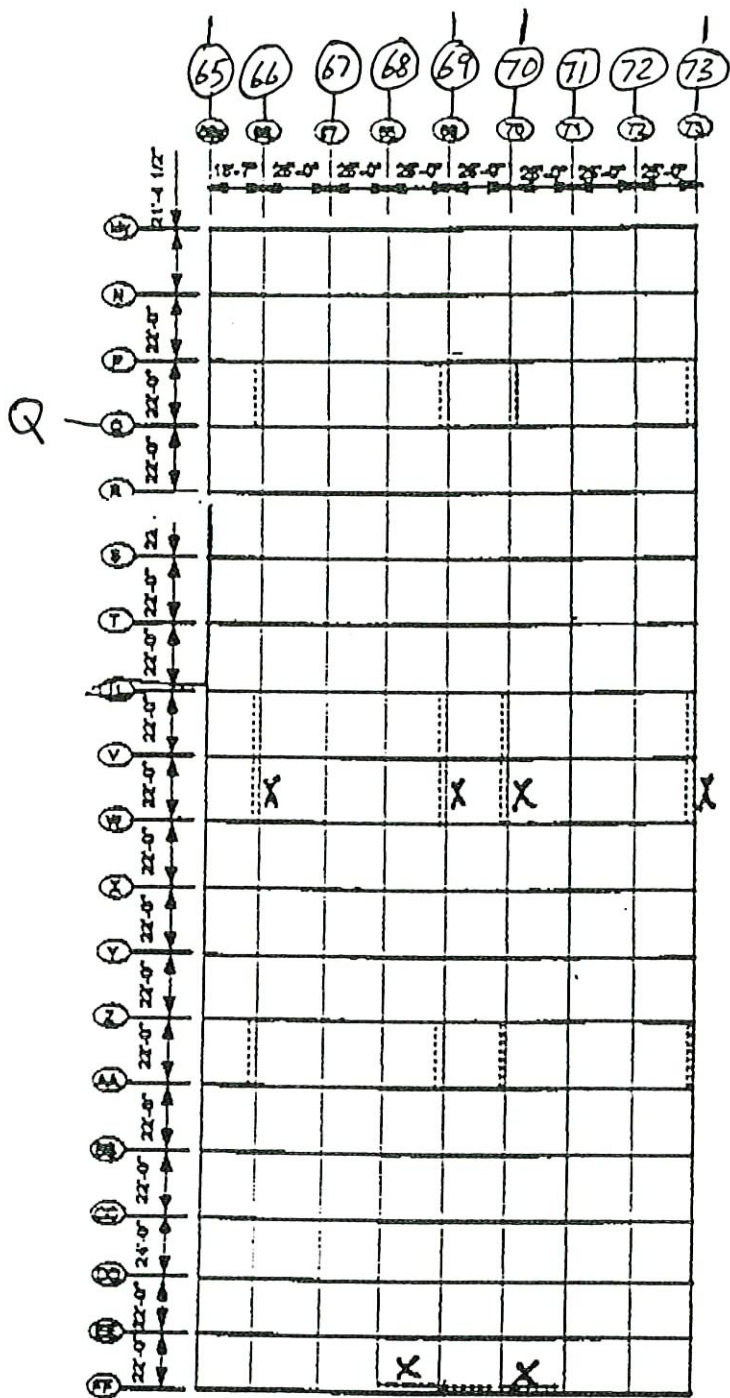
Horizontal Response  
Based on 3-D Model of Building

Mode	Freq. (Hz.)	% Mass Part.	Dir.	% Mass Part.	Dir.
1.	0.309	73.39	N-S	0.00	E-W
2	0.892	6.98	N-S	0.53	E-W
3	0.928	0.00	N-S	98.01	E-W
4	0.964	8.05	N-S	0.00	E-W
5	1.039	2.70	N-S	0.00	E-W
6	1.460	2.35	N-S	0.00	E-W
7	1.559	4.96	N-S	0.00	E-W

Vertical Response  
Based on 2-D Section Along Column Line Q

Mode	Frequency (Hz.)	% Mass Part.
1	10.3	28.9
2	10.5	25.7
5	11.8	22.0
7	12.7	12.1
8	15.3	7.5

Building X-330 Seismic Response  
Table 4.1.1-5

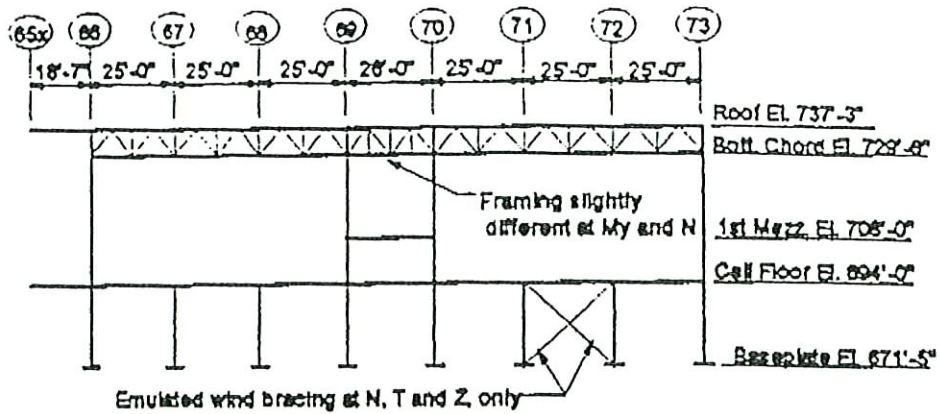


X - bellow cell floor

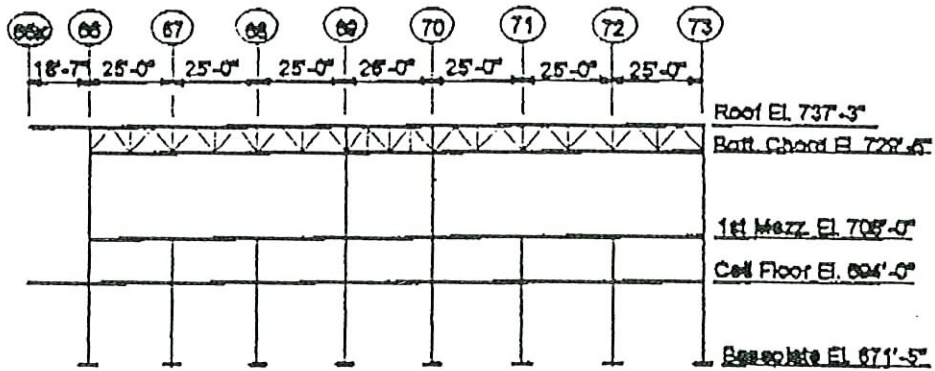
} 1st MEZZANINE

Building X-330 Typical Building Framing

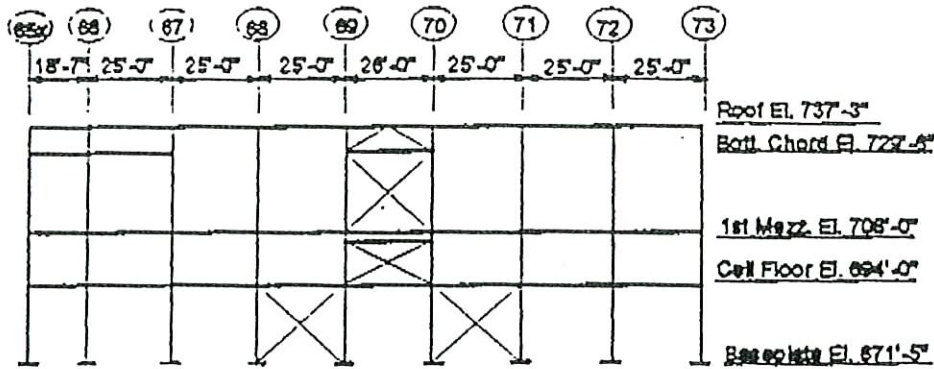
Figure 4.1.1-4



Typical N/S Section Along Column Lines  
My, N, P, QR, S, T, U, V, W, X, Y, Z, AA, BB and CC  
(As noted)

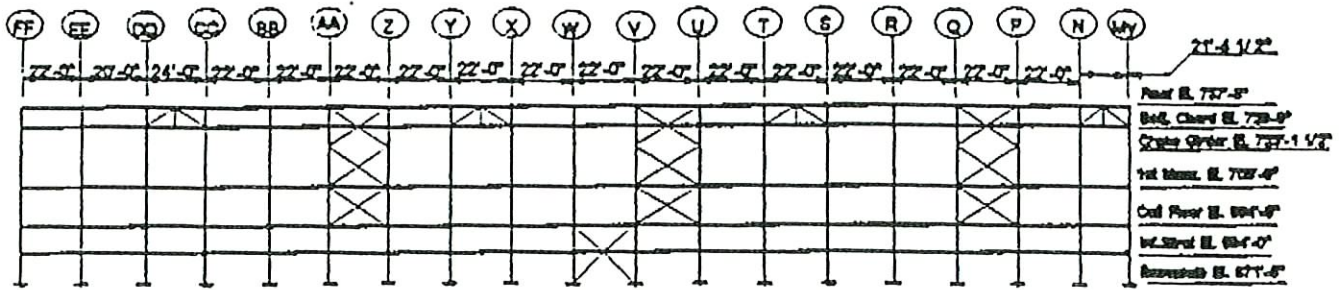


Typical N/S Sections Along Column Lines DD and EE

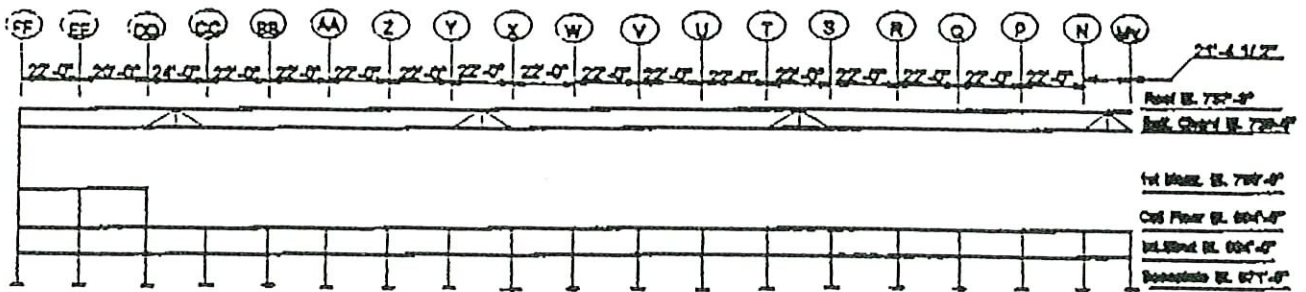


N/S Section Along Column Line FF

Building X-330 Typical Building Framing  
Figure 4.1.1-4 (continued)



Typical E/W Sections Along Column Lines 68, 69, 70 and 73



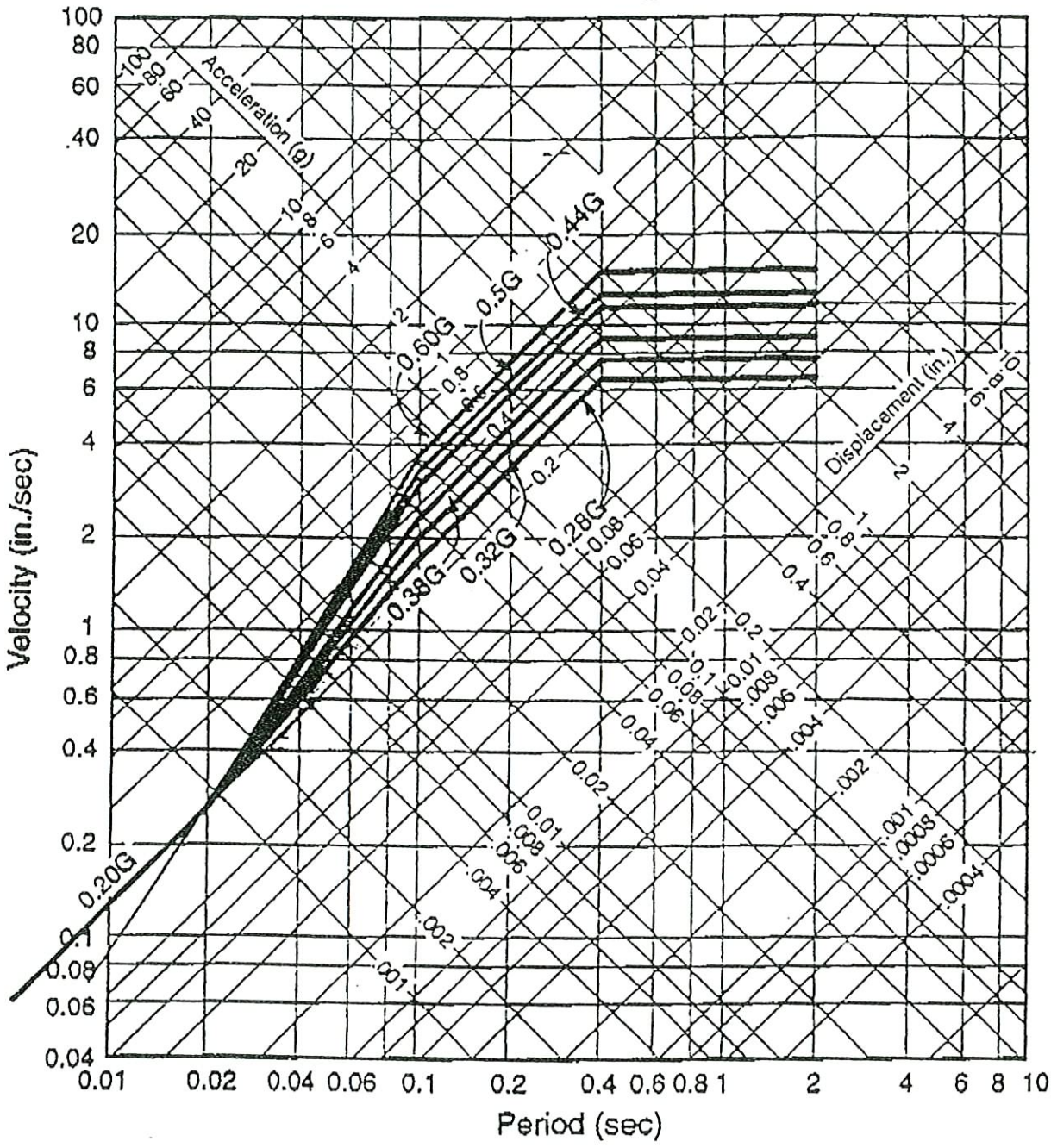
Typical E/W Sections Along Column Lines 67, 68, 71 and 72

Building X-330 Typical Building Framing

Figure 4.1.1-4 (continued)

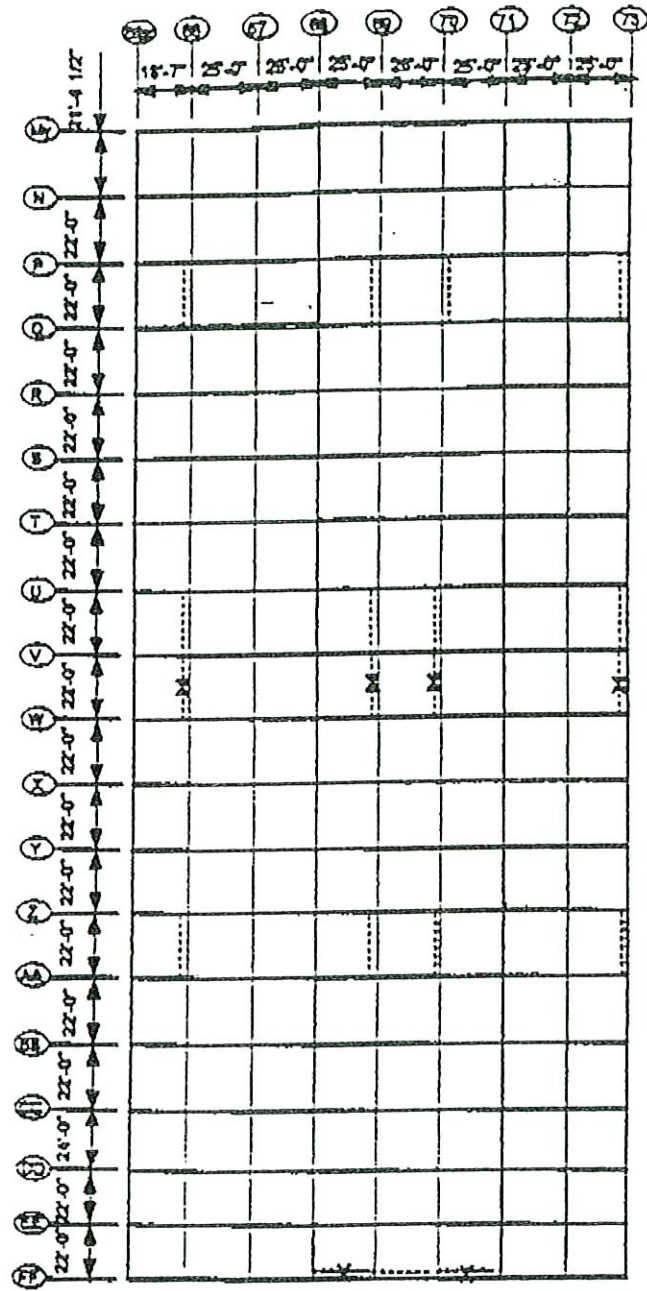


Damping Ratios - 2, 5, 7, 10, 12, and 15% *evaluated at.*



**PADUCAH - 500 YEAR UNIFORM HAZARD  
GROUND SURFACE RESPONSE  
SPECTRA - HORIZONTAL MOTION**





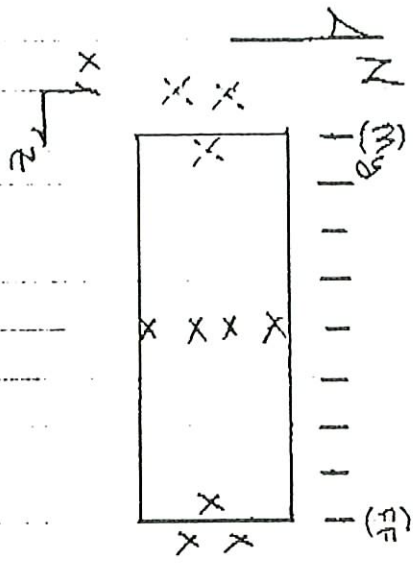
Module Plan View  
 → N

- ..... Denotes main vertical bracing above cell floor
- X--- Denotes main vertical bracing below cell floor

③ Typical Building Framing

# GENERAL DESIGN AND COMPUTATION SHEET

JOB: C-331 MOD STAIRS  
 DATE: \_\_\_\_\_ SHEET: \_\_\_\_\_ of \_\_\_\_\_  
 ESO NO. C-848401  
 CHECKED BY: \_\_\_\_\_



2 g input spectra 500 g R  
 x - existing cross bracing  
 x - add cross bracing

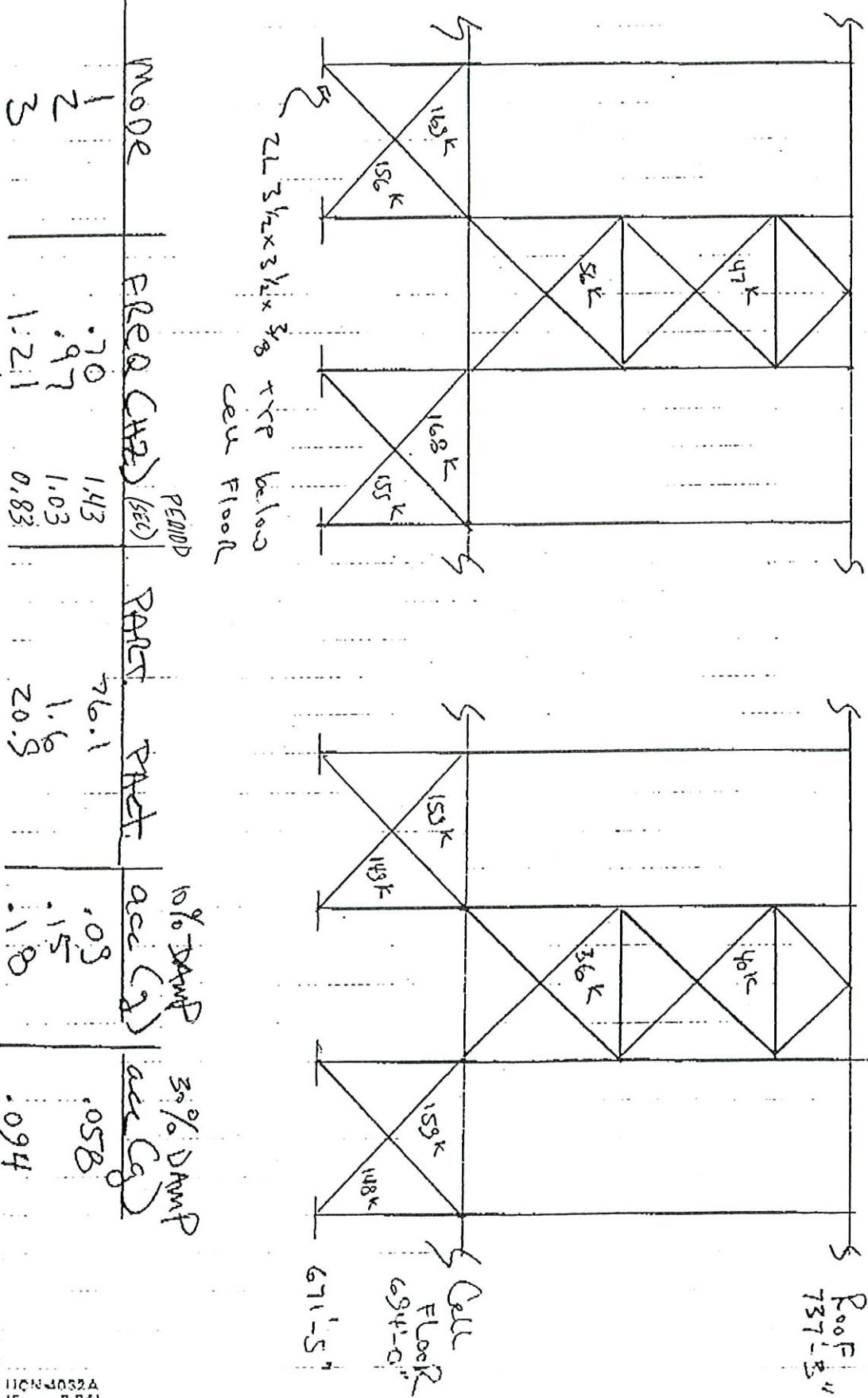
Condition	As-built	My braced to cell Floor	My braced to Roof	My braced to Roof + 30% Damped input spectra direct
Displ (Rss) Roof	11.7"	7.3"	4.4"	2.23"
Displ (Rss) Cell	6.2"	2.1"	2.1"	1.1"
BASE Reaction (N-S)	160 k ↑	297 k ↑	328 k ↑	137 k ↑
BASE Reaction (E-W)	770 k ↑	596 k ↑	601 k ↑	257 k ↑
BRACING (N-S)	368 k	\$81 k	609 k	325 k
BRACING (E-W)	1244 k	997 k	1002 k	523 k
BRACING (N-S)	146 k	180 k	216 k	112 k
BRACING (E-W)				

Above Cell Floor      Below Cell Floor



# GENERAL DESIGN AND COMPUTATION SHEET

JOB <b>C-331 MOD STUDY</b>	DATE	SHEET of
ESO NO. <b>CE848401</b>	COMPUTED BY <b>R. K. Kumar</b>	CHECKED BY



FF  
(Existing)

MG  
(Modified)

MODE	PERIOD (SEC)	PERCENT DAMP	PERCENT ACC (g)	PERCENT ACC (g)
1	.70	10% DAMP	.08	.058
2	.97	3% DAMP	.15	
3	1.21		.18	
				.094

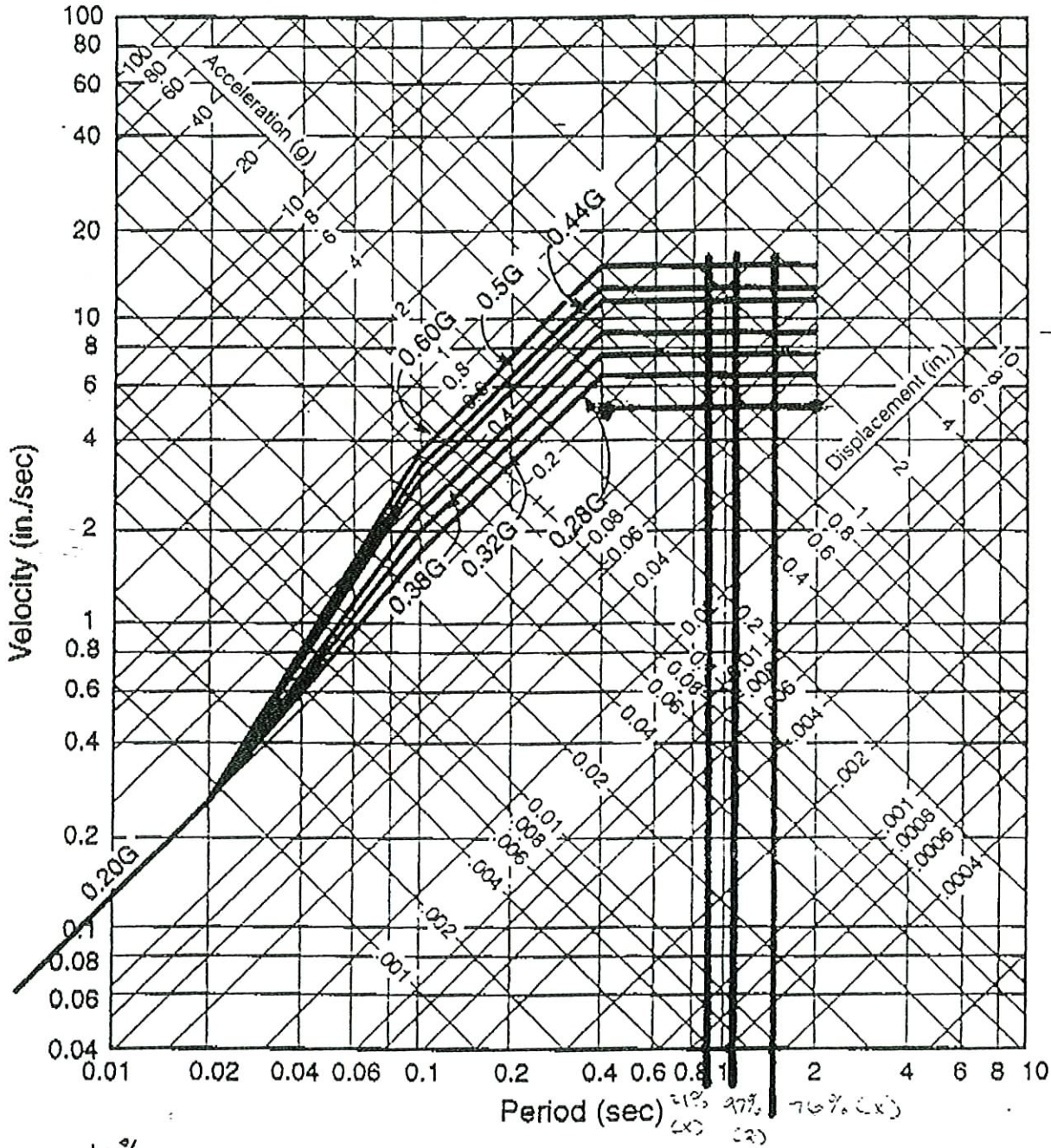


10% to 30%  $\approx$  35% Reductions

$V_{@10\%} = 9 \text{ in./sec}$

$V_{@30\%} \approx 5.9 \text{ in./sec}$

Damping Ratios - 2, 5, 7, 10, 12, and 15%



9  
35.35

	% mass	10% Acc (%)
100		
3	7.5	.10
5	37.5	.10
32	20.3	.16

**PADUCAH - 500 YEAR UNIFORM HAZARD  
GROUND SURFACE RESPONSE  
SPECTRA - HORIZONTAL MOTION**



Y-GA 94-57 lhm

may be used to roof

11/29/94

INITIAL REVIEW

DAMPING VS. ISOLATING STUDY

MARTIN MARIETTA OAK RIDGE PLANT  
BLDG X-330

CRAIG W WINTERS

OAK RIDGE Y-12 PLANT

11/29/94  
CWW

BUILDING X-330

① CONSIDER N-S DIRECTION

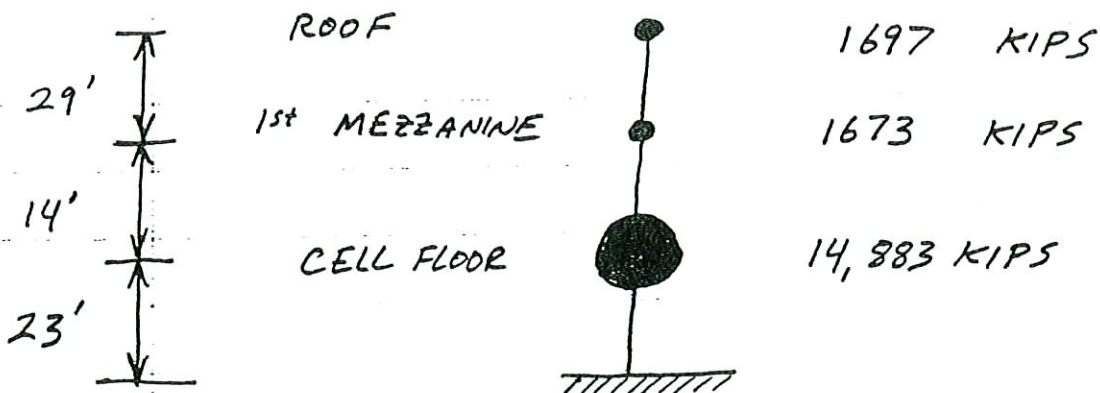
FIRST MODE $\Rightarrow$	1	$f = 0.309 \text{ HZ}$	73.39% MR
SECOND MODE $\Rightarrow$	4	$f = 0.964 \text{ HZ}$	8.05% MR

MOST EFFECT FROM MODE 1

$$T_1 = \frac{1}{0.309} = 3.24 \text{ SEC}$$

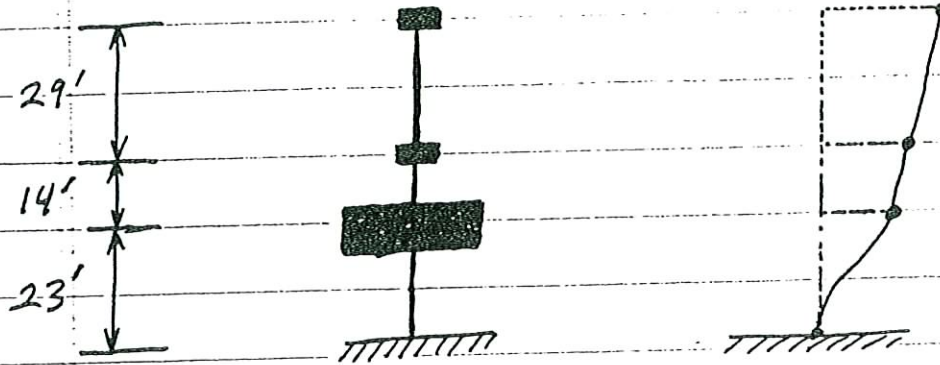
$$W_{\text{TOTAL}} = 18,253 \text{ KIPS}$$

BUT, LETS LOOK AT WEIGHT DISTRIBUTION:



16" DEFLECTION





BASE ISOLATION UNNECESSARY

$$\text{PERIOD} = 3.24 \text{ SEC}$$

\* NOT APPROPRIATE TO SHIFT PERIOD HIGHER  
SINCE WE ARE ALREADY AT OR ABOVE  
TYPICAL PERIODS THAT AN ISOLATION SYSTEM  
WILL SHIFT THE STRUCTURE TO.

∴ STRUCTURE NEEDS DAMPING!

MOST DAMPERS WILL BE PLACED IN DIAGONAL  
BRACING FROM BASE TO FIRST FLOOR - CELL FLOOR.

SOME DAMPERS PLACED BETWEEN 1st MEZZANINE  
AND ROOF DUE TO THE HEIGHT (29') MAYBE ONLY A FEW

SMALL AMOUNT OR NO DAMPERS PLACED BETWEEN  
CELL FLOOR AND 1st MEZZANINE. SUSPECT LITTLE  
RELATIVE DISPLACEMENT + VELOCITIES HERE

② CONSIDER E-W DIRECTION

FIRST MODE  $\Rightarrow$  3  $f = 0.928$  98.01% MASS

EFFECTS COMING COMPLETELY FROM THIS <sup>FIRST</sup> MODE

$$T_1 = \frac{1}{0.928} = 1.08 \text{ SEC}$$

AGAIN, SAME WEIGHT DISTRIBUTION AS N-S DIRECTION

\* PERIOD IS SUFFICIENTLY HIGH

$\therefore$  PROVIDE DAMPING

- AGAIN, DAMPERS PLACED IN LEVELS AS BEFORE
- MAY WANT TO PROVIDE HIGHER DAMPING IN THIS DIRECTION SINCE OUR PERIOD IS  $\frac{1}{3}$  THAT OF THE N-S DIRECTION

1/10/95

## DAMPING ANALYSIS

PROVIDE 20% OF CRITICAL  
DAMPING WITH FLUID VISCOUS DAMPERS

HAND CALCULATIONS USING THEORY FROM  
NCEER-92-0032 REPORT. PERTINENT  
PAGES INCLUDED AT END OF THIS SECTION

MARTIN MARIETTA OAK RIDGE PLANT  
BLDG X-330

CRAIG W. WINTERS



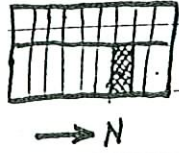
MARTIN - MARIETTA

OAK RIDGE Y-12 PLANT BLDG X-330

1/13/95  
CWN

**ANALYSIS**

BUILDING LAYOUT COMPOSED OF 22 SIMILAR SUBFRAMES SEPARATED BY FLEXIBLE INTERFACES.

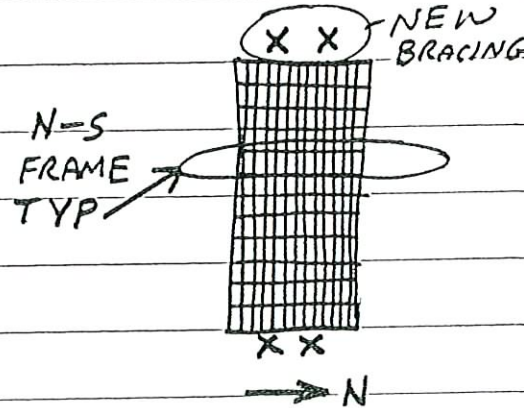


ASSUMPTION 1: NO INTERACTION BETWEEN SUBFRAMES

∴ CONSIDER 1 SUBFRAME ONLY AND PROVIDE RQD DAMPING

N-S DIRECTION

WITH NEW BRACING,



$$T_1 = 1.21 \text{ SEC}$$

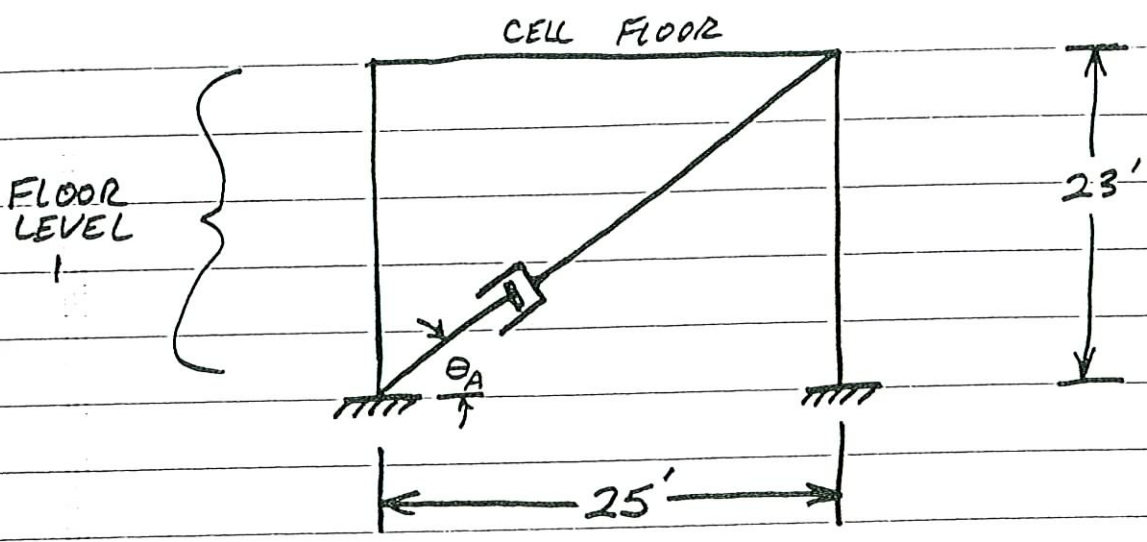
$$\omega_1 = 2\pi f_1 = 2\pi \frac{1}{T_1} = 5.19 \text{ rad/sec}$$

NORMALIZED

		$\phi_1$	$W_1$	$M_1$
FLOOR 3	ROOF	+1.0000	1697 <sup>k</sup>	4.39 $\frac{\text{KIP} \cdot \text{S}^2}{\text{IN}}$
FLOOR 2	1 <sup>st</sup> MEZZANINE	+0.6058	1673 <sup>k</sup>	4.33 "
FLOOR 1	CELL FLOOR	+0.3947	14,833 <sup>k</sup>	38.39 "

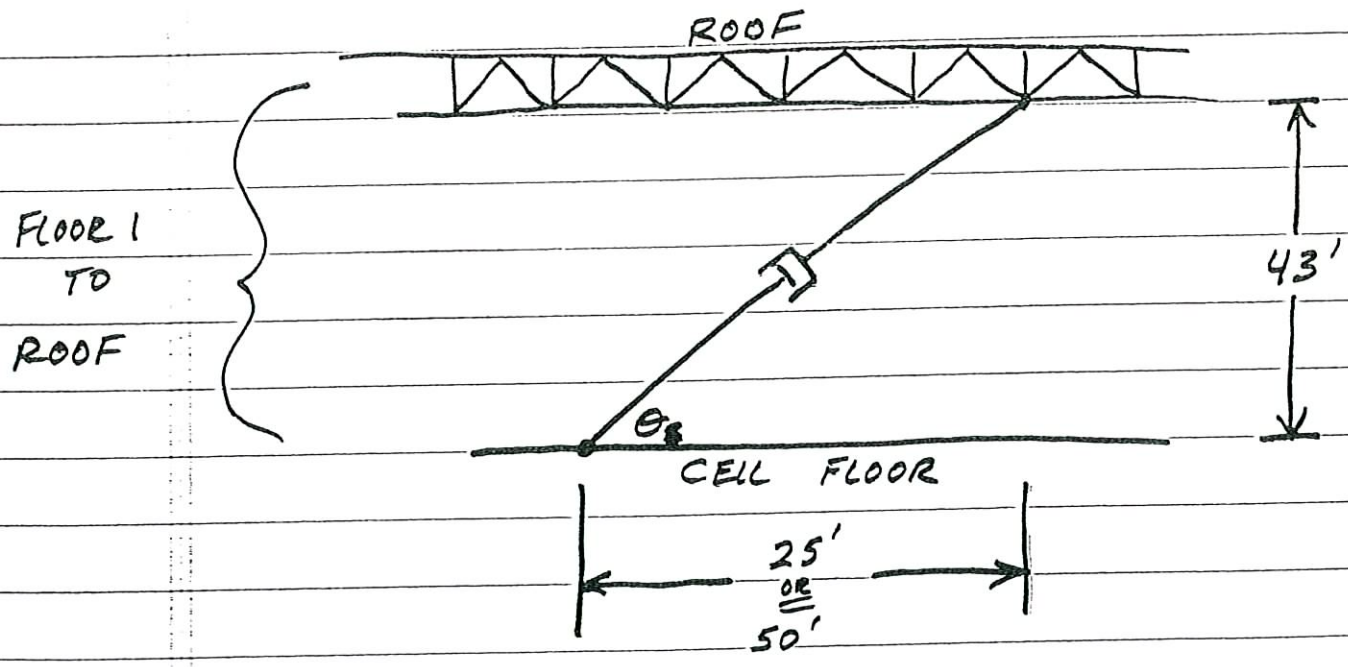
$$\sum_j M_j \phi_j^2 = 4.39 + 1.59 + 5.98 = 11.96 \frac{\text{KIP} \cdot \text{SEC}^2}{\text{IN}}$$

CALCULATE DAMPER ANGLES OF ORIENTATION



$$\theta_A = \tan^{-1} \frac{23}{25} = 42.6^\circ$$

$$\cos^2 \theta_A = 0.5418$$



$$\theta_B = \tan^{-1} \frac{43}{25} = 59.8^\circ \quad \leftarrow \text{TRY THIS}$$

$$\tan^{-1} \frac{43}{50} = 40.7^\circ$$

$$\cos^2 \theta_B = 0.2530$$



PER EQUATION (6-11) P 6-20 NCEER-92-0032  
 APPLY 30% OF CRITICAL DAMPING TO STRUCTURE  
 WITH ASSUMPTION THAT BUILDING PROVIDES 10%  
 OF CRITICAL DAMPING.

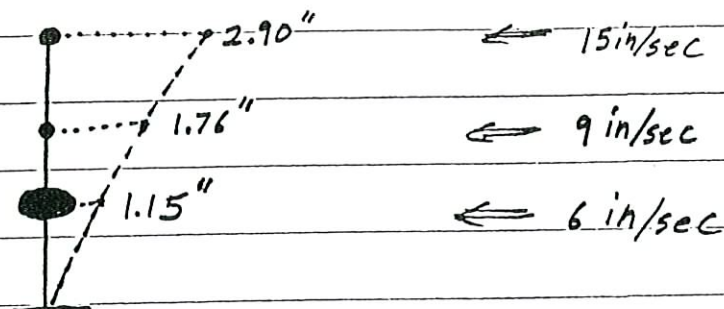
$$30\% = 10\% + \frac{1}{2} \frac{\sum_j C_j \left[ (0.5418)(.3947)^2 + (.2530)(.6053) \right]}{\left( 5.19 \frac{\text{rad}}{\text{sec}} \right) \left( 11.96 \frac{\text{K} \cdot \text{s}^2}{\text{in}} \right)}$$

$$.20 = \frac{1}{2} \frac{.1771 C_j}{62.07}$$

$$C_j = 140.2 \frac{\text{KIP} \cdot \text{sec}}{\text{in}}$$

CALCULATE REQ'D OUTPUT FORCE + VELOCITY  
 $(F = CV)$

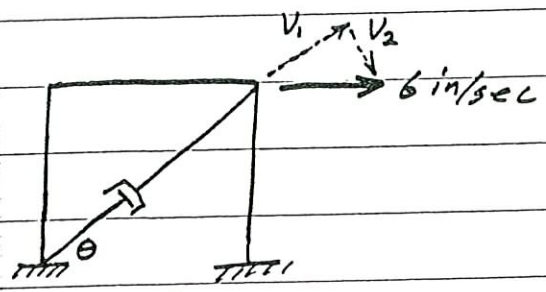
N-S  
 DISPLACEMENT  
 PROFILE



$$\begin{aligned} \text{PSEUDO VELOCITY} &= \omega_1 \Delta \\ &= (5.19)(\Delta) \end{aligned}$$

FIND VELOCITY ALONG DAMPER DIRECTION

(CELL)  
FIRST FLOOR

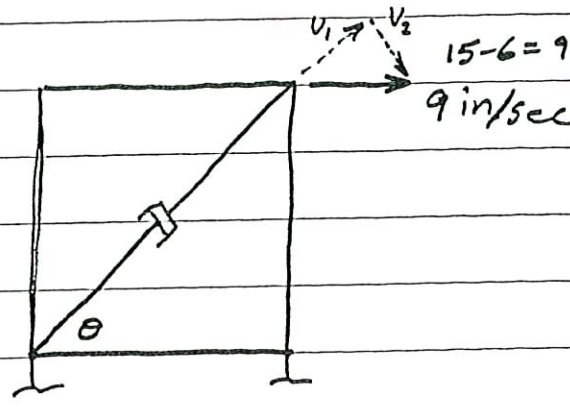


$\theta = 42.6^\circ$

$\cos \theta = \frac{V_1}{6 \text{ in/sec}}$

$V_1 = 4.4 \text{ in/sec}$

CELL FLOOR TO ROOF



$\theta = 59.8^\circ$

$\cos \theta = \frac{V_1}{9 \text{ in/sec}}$

$V_1 = 4.5 \text{ in/sec}$

$F = CV$

$F = (140.2)(4.4) = 620 \text{ KIPS}$

$F = CV$

$F = (140.2)(4.5) = 630 \text{ KIPS}$

USE 13 pcs 50 KIP DAMPER

WITH  $C = 140.2 \frac{\text{K}\cdot\text{S}}{\text{IN}}$

USE 13 pcs 50 KIP

WITH  $C = 140.2 \frac{\text{K}\cdot\text{S}}{\text{IN}}$

TOTAL = 26 pcs 50 KIP DAMPERS SET WITH  $C = 140.2 \frac{\text{K}\cdot\text{S}}{\text{IN}}$   
 $V_{\text{max}} \approx 4.5 \text{ in/sec}$       STROKE =  $\pm 2''$

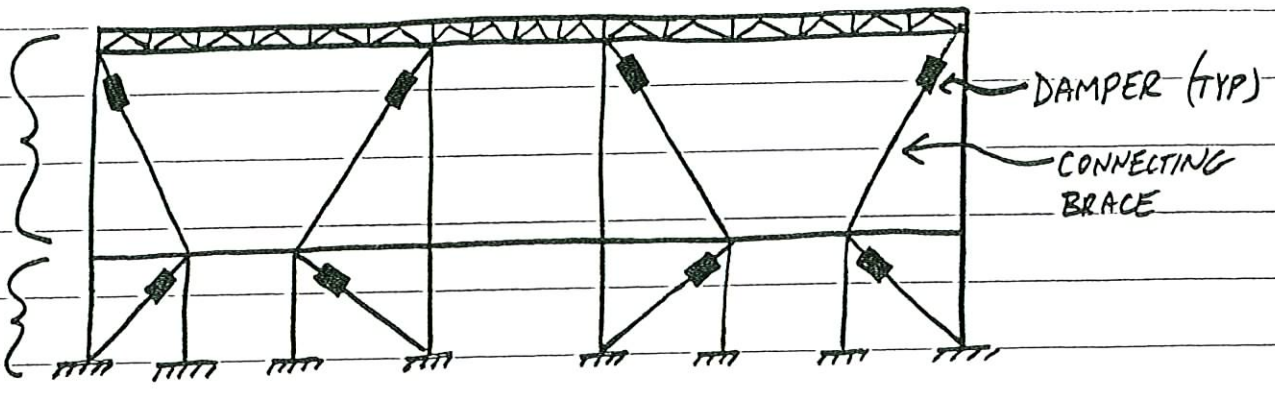
STROKE:  $(2.90 - 1.15) \cos 59.8 = 0.88''$

$1.15 \cos 42.6 = 0.85''$

USE  $\pm 2''$  SET @ MID-STROKE

DAMPERS  
PLACED FROM  
CELL FLOOR TO  
ROOF

DAMPERS  
PLACED IN FIRST  
LEVEL



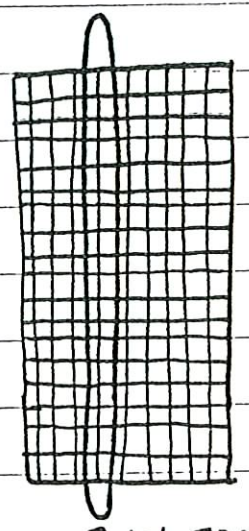
N-S FRAME



E - W DIRECTION

$T_1 = 1.04 \text{ SEC}$

$\omega_1 = 2\pi \frac{1}{T_1} = 6.04 \text{ rad/sec}$



E-W FRAME

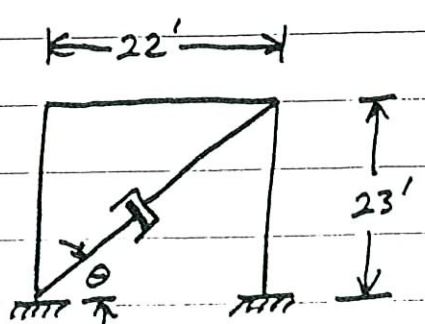
BASED ON MODE SHAPES,  
WE HAVE SEVERE SOFT FIRST STORY.

∴ PLACE ALL DAMPERS IN FIRST  
STORY DIAGONAL BRACING.

		NORMALIZED $\phi$	$W_1$	$M_1$
FLOOR 3	ROOF	1.0000	1697 <sup>K</sup>	4.39
FLOOR 2	1 <sup>st</sup> MEZZANINE	0.9487	1673 <sup>K</sup>	4.33
FLOOR 1	CELL FLOOR	0.9096	14833 <sup>K</sup>	38.39

$\sum_j M_j \phi_j^2 = 4.39 + 3.90 + 31.76 = 40.05 \frac{\text{KIP} \cdot \text{SEC}^2}{\text{IN}}$

DAMPER ANGLE OF ORIENTATION :



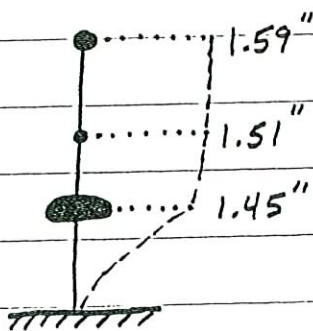
$\theta = \tan^{-1} \frac{23}{22} = 46.3^\circ$   
 $\cos^2 \theta = 0.4773$

USING EQ (6-11),

$$30\% = 10\% + \frac{1}{2} \frac{\sum C_j [(0.4773)(0.9096)^2]}{(6.04 \frac{\text{rad}}{\text{sec}})(40.05 \frac{\text{KIP}\cdot\text{sec}^2}{\text{in}})}$$

$$C_j = 245.0 \frac{\text{KIP}\cdot\text{sec}}{\text{in}}$$

E-W  
DISPLACEMENT  
PROFILE



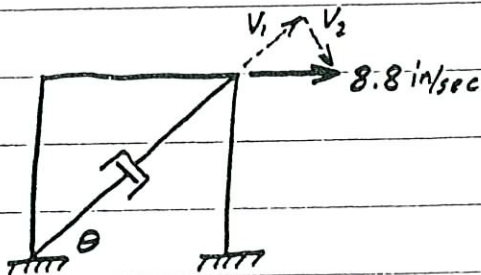
9.60 in/sec

9.12 in/sec

8.78 in/sec

PSEUDO VELOCITY =  $\omega, \Delta = (6.04) \Delta$

FIRST (CELL) FLOOR DAMPERS ONLY - FIND VELOCITY ALONG DAMPER DIRECTION:



$$\cos \theta = \frac{V_1}{8.8 \text{ in/sec}}$$

$$V_1 = 6.0 \text{ in/sec}$$

$$\theta = 46.3^\circ$$

$$F = CV$$

$$F = (245)(6.0) = 1470 \text{ KIPS}$$

STROKE REQUIRED:

$$\Delta = 1.45'' \cos 46.3 = 1.002'' \quad \therefore \text{NEED } \pm 1.002''$$

PROVIDE  $\pm 2''$ , USE MIDDLE OF STROKE

USE: 30 pcs 50 KIP DAMPERS SET WITH

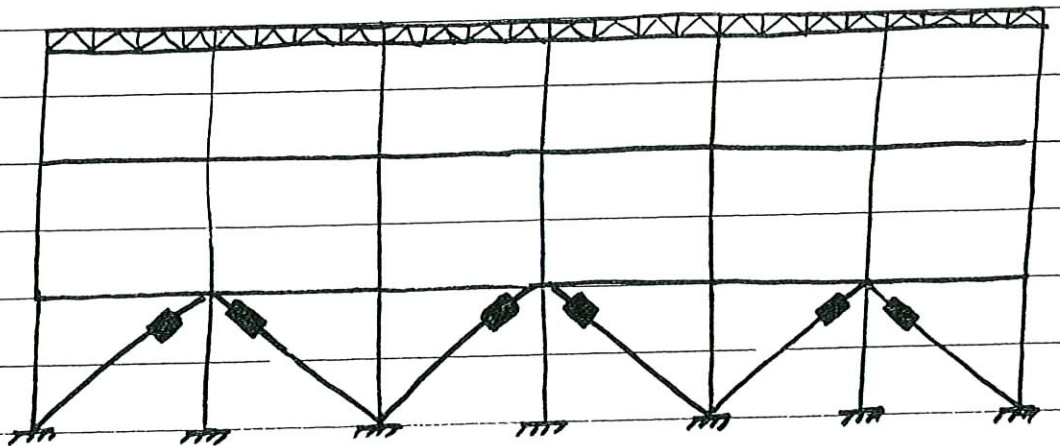
$$C = 245 \frac{\text{KIP S}}{\text{IN}}$$

$$V_{\text{max}} = 6.0 \text{ in/sec}$$

$\pm 2''$  STROKE

E-W FRAME

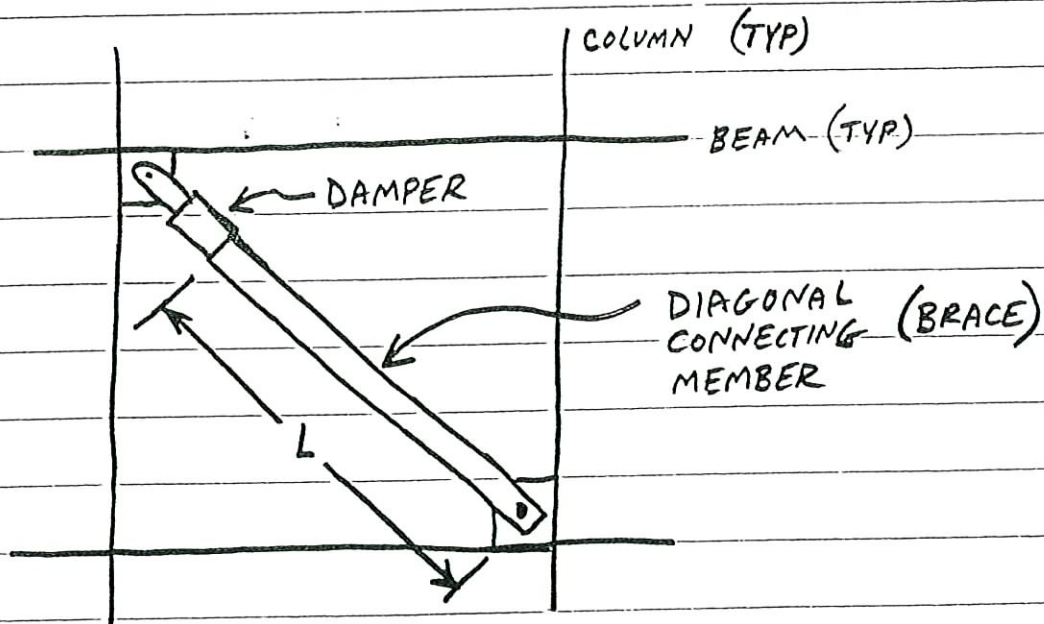
DAMPERS  
IN FIRST  
LEVEL ONLY





- ① THE PREVIOUS ANALYSIS ASSUMES DAMPING IN BOTH DIRECTIONS. THEREFORE, DIAGONAL CONNECTING MEMBERS FOR BEAM-COLUMN JOINTS TO DAMPERS MUST BE SUFFICIENTLY LARGE TO PREVENT BUCKLING. ALSO, X-SECTION MUST BE LARGE SUCH THAT THE STRAIN IN THE CONNECTING BRACE IS NEGLIGIBLE COMPARED WITH THE DAMPER STROKE USED. GENERALLY, KEEP STRAIN BELOW 5% OF STROKE;  $0.05 \times 0.8'' = .04''$

$$\therefore \Delta L_{\text{BRACE}} \leq 0.04''$$



$$L \Rightarrow \sqrt{25^2 + 23^2} - 2' = 32' = 384''$$

$$\sqrt{25^2 + 43^2} - 2' = 47\frac{1}{2}' = 570''$$

$$\sqrt{22^2 + 23^2} - 2' = 30' = 360''$$

$$\epsilon = \frac{\Delta L}{L} = \frac{.04''}{570''} = 7.02 \times 10^{-5} \quad (\text{WORST CASE})$$

USING 50 KIP DAMPER, CALCULATE  
X-SECTION AREA REQUIRED:

$$\sigma = E \epsilon$$

$$\frac{P}{A} = E \epsilon$$

$$\frac{50 \text{ KIP}}{A} = (29,000 \text{ ksi}) (7.02 \times 10^{-5})$$

$$A = 24.6 \text{ in}^2 \quad \text{FOR LONGEST BRACE}$$

(10" DIA, SCHED 120 PIPE WORKS) (WORST CASE)

$$A = 16.6 \text{ in}^2 \quad \text{OKAY FOR OTHER TWO BRACE}$$

(8" DIA, SCHED 120 PIPE WORKS)

BRACES ARE FAIRLY LARGE, BUT NECESSARY FOR  
DAMPER TO UTILIZE MAXIMUM DEFLECTION OF  
STRUCTURE.



N-5

KRCCO.OUT

Generalized macs (k-sec<sup>2</sup>/in) ./ 4.9965E+00  
 Generalized stiffness (k/in) ./ 1.5850E+03

Mode shape: 1  $(\phi_i - \phi_{i-1})$

Floor	Ordinate
01	+0.3947
02	+0.6058
03	+1.0000

GFD } 0.3947  
 CEU } 0.2111  
 1<sup>st</sup> MEZ } 0.6053  
 ROOF } 0.3942

Mode shape: 2

Floor	Ordinate
01	-0.2956
02	+0.0389
03	+1.0000

Mode shape: 3

Floor	Ordinate
01	-0.0923
02	+1.0000
03	-0.2777

Mode number: 1

Floor	Disp(in.)	Force(kips)	Shear(kips)	Story Acc(g's)	Floor Drift(in.)
-------	-----------	-------------	-------------	----------------	------------------

E-W

XR01-QJT

Generalized mass (k-sec<sup>2</sup>/in) ./ 5.0103E+00  
Generalized stiffness (k/in) ./ 1.4736E+04

$(\phi_i - \phi_{i-1})$

Mode shape: 1

Floor	Ordinate
01	+0.9096
02	+0.9487
03	+1.0000

GND  
 CELL  
 1st MEZ  
 ROOF

0.9096

0.0904

Mode shape: 2

Floor	Ordinate
01	-0.1514
02	+0.2218
03	+1.0000

Mode shape: 3

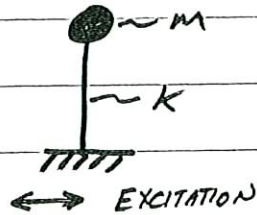
Floor	Ordinate
01	-0.0770
02	+1.0000
03	-0.3209

Mode number: 1

Floor	Disp(in.)	Floor Force(kips)	Story Shear(kips)	Floor Acc(g's)	Story Drift(in.)
01	-0.0770				
02	+1.0000				
03	-0.3209				

# ANALYSIS CHECK

E-W DIRECTION (CAN EASILY BE SDOF MODEL)



$$W = 1697 + 1673 + 14833 = 18,203$$

$$m = \frac{W}{g} = 47.11 \frac{\text{k} \cdot \text{sec}^2}{\text{in}}$$

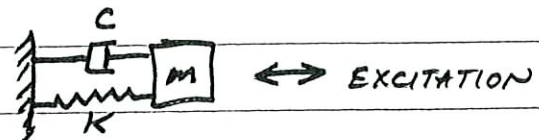
$$T = 1.04 \text{ sec} \Rightarrow \omega = 6.04 \text{ rad/sec}$$

$$\zeta = \frac{c}{2m\omega}$$

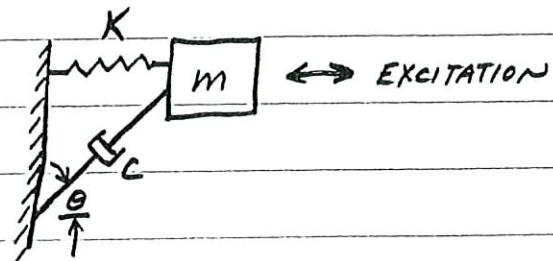
$$\zeta = \frac{245 \frac{\text{k} \cdot \text{s}}{\text{in}}}{2(47.11 \frac{\text{k} \cdot \text{s}^2}{\text{in}})(6.04 \text{ rad/s})} = 43\% \text{ OF CRITICAL}$$

BUT, THIS EQUATION DOES NOT TAKE INTO ACCOUNT THE  $\theta$ .

ABOVE EQ ASSUMES:



BUT WE HAVE:



$\therefore$  MUST MULTIPLY BY  $\cos^2 \theta$

$$\theta = 46.3^\circ \Rightarrow \cos^2 \theta = (0.69)^2 = 0.4773$$

$$\zeta = 0.4773(43\%) = 20.5\% \quad \checkmark$$



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# Experimental and Analytical Investigation of Seismic Response of Structures with Supplemental Fluid Viscous Dampers

by

M. C. Constantinou and M. D. Symans

State University of New York at Buffalo

Department of Civil Engineering

Buffalo, New York 14260

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The application of the response spectrum analysis method requires that estimates of the structural properties are available.

### 6.3.1 Approximate Determination of Structural Properties

Approximate methods for the determination of the frequencies, mode shapes and damping ratios of non-classically damped structures have been successfully applied in problems involving soil-structure interaction (e.g., Novak 1983; Constantinou 1987). Veletsos (1986) presented a comprehensive treatment of the method.

The method starts with the assumption that frequencies and mode shapes of the non-classically damped structure are identical to those of the undamped structure. Typically, these quantities are determined in a standard eigenvalue analysis.

The modal damping ratios are determined from an analysis involving energy considerations. The damping ratio in the  $k$ -th mode of vibration may be expressed as

$$\xi_k = \xi_{str.} + \frac{W_k}{4\pi L_k} \quad (6-6)$$

where  $\xi_{str.}$  is the damping ratio due to damping inherent to the structure,  $W_k$  is the work done by the dampers in a single cycle of motion, and  $L_k$  is the maximum strain energy.  $W_k$  may be expressed as

$$W_k = \sum_j \int_0^{T_k} P_j d(u_j - u_{j-1}) \quad (6-7)$$

where  $P_j$  is the horizontal component of the force in the dampers at the  $j$ -th story, and  $u_j$  is the modal displacement of the  $j$ -th floor. For the case of purely viscous dampers, it can be shown that

$$P_j = C_j \cos^2 \theta_j (\phi_j - \phi_{j-1}) \omega_k \cos(\omega_k t) \quad (6-8)$$

where  $C_j$  is the combined damping coefficient of the dampers at the  $j$ -th story,  $\theta_j$  is the angle of inclination of the dampers at the  $j$ -th story,  $\phi_j$  is the modal displacement of the  $j$ -th floor in the  $k$ -th mode of vibration, and  $\omega_k$  is the frequency of vibration in the  $k$ -th mode. Combining Equations 6-7 and 6-8,  $W_k$  can be written as

$$W_k = \pi \omega_k \sum_j C_j \cos^2 \theta_j (\phi_j - \phi_{j-1})^2 \quad (6-9)$$

The maximum strain energy is equal to the maximum kinetic energy, so that

$$L_k = (KE)_{MAX} = \frac{1}{2} \sum_j m_j \phi_j^2 \omega_k^2 \quad (6-10)$$

Combining Equations 6-6, 6-9 and 6-10, the damping ratio of the structure in the  $k$ -th mode of vibration is determined to be

$$\xi_k = \xi_{str,k} + \frac{1}{2} \frac{\sum_j C_j \cos^2 \theta_j (\phi_j - \phi_{j-1})^2}{\omega_k \sum_j m_j \phi_j^2} \quad (6-11)$$

It is clear from Equation 6-11 that in order to have the greatest contribution to the modal damping ratio, the dampers should be placed at story levels where the modal interstory drift ( $\phi_j - \phi_{j-1}$ ) is maximum.

The accuracy of the simple energy approach in determining the damping ratios of the tested structures is demonstrated in Tables 6-I and 6-II. The tables include the damping ratios calculated by the complex eigenvalue approach of Section 4 wherein the calibrated rigorous Maxwell model is utilized for the fluid dampers. The calculation was repeated by utilizing the simple viscous model and,

TABLE 6-I Comparison of Damping Ratios of One-Story Model Structure

STRUCTURE	NUMBER OF DAMPERS	RIGOROUS METHOD MAXWELL MODEL	RIGOROUS METHOD VISCOUS MODEL	ENERGY APPROACH VISCOUS MODEL
UNSTIFFENED	2	0.284	0.280	0.280
STIFFENED		0.193	0.192	0.192
UNSTIFFENED	4	0.577	0.554	0.554
STIFFENED		0.374	0.363	0.363

TABLE 6-II Comparison of Damping Ratios of 3-story Model Structure

NUMBER OF DAMPERS	RIGOROUS METHOD MAXWELL MODEL			RIGOROUS METHOD VISCOUS MODEL			ENERGY APPROACH VISCOUS MODEL		
	MODE 1	MODE 2	MODE 3	MODE 1	MODE 2	MODE 3	MODE 1	MODE 2	MODE 3
2	0.099	0.147	0.050	0.100	0.154	0.049	0.100	0.149	0.051
4	0.177	0.319	0.113	0.183	0.326	0.081	0.183	0.291	0.098
6	0.194	0.447	0.380	0.193	0.428	0.490	0.193	0.428	0.490



thus, solving exactly the eigenvalue problem of the non-classically damped structure ( $\lambda$  was set equal to zero). Finally, the procedure of Equation 6-11 was employed.

The results demonstrate that the damping in the fundamental mode is predicted very well by the energy approach. In addition, the energy approach provides reasonable approximations to the damping ratios of the higher modes. The error in the calculation of the higher mode damping ratios is due to neglect of the stiffening effect of the tested fluid dampers at frequencies exceeding about 4 Hz.

### 6.3.2 Determination of Peak Response

The determination of the peak structural response to an excitation described by a response spectrum requires that the peak response in each significant mode of vibration be evaluated first (Clough 1975). The required mode shapes, frequencies and damping ratios are determined by the procedures described in Section 6.3.1. The calculated peak modal responses are then combined by an appropriate combination rule to give estimates of the peak response.

The only complexity in the application of this approach is that of constructing high damping response spectra from the usually specified 5%-damped spectra. A recent study on this problem has been reported by Wu (1989). However, it may be appropriate to include de-amplification factors of design spectra at high damping in future design requirements of structures with supplemental damping devices. This will ensure uniformity, reasonable conservatism and avoidance of gross errors.